

**Topology of the polarization field in ferroelectric nanowires from first principles**Jiawang Hong,<sup>1,2</sup> G. Catalan,<sup>1,3</sup> D. N. Fang,<sup>2,4</sup> Emilio Artacho,<sup>1,5</sup> and J. F. Scott<sup>1,6</sup><sup>1</sup>*Department of Earth Sciences, University of Cambridge, Downing Street, Cambridge CB2 3EQ, United Kingdom*<sup>2</sup>*AML, Department of Engineering Mechanics, Tsinghua University, Beijing 100084, People's Republic of China*<sup>3</sup>*ICREA and Centre d'Investigació en Nanociència i Nanotecnologia (CIN2), Campus UAB, Bellaterra, Spain*<sup>4</sup>*LTCS, College of Engineering, Peking University, Beijing 100084, People's Republic of China*<sup>5</sup>*Donostia International Physics Centre, Universidad del País Vasco, 20080 San Sebastian, Spain*<sup>6</sup>*Cavendish Laboratory, University of Cambridge, JJ Thomson Avenue, Cambridge CB3 0HE, United Kingdom*

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The behavior of the cross-sectional polarization field is explored for arrays of thin nanowires of barium titanate from first principles. Topological defects of different winding numbers have been obtained, beyond the known textures in ferroelectric nanostructures. They result from the inward accommodation of patterns imposed at the surface of the wire by surface and edge effects. Close to a topological defect, the polarization field orients out of the basal plane in some cases, maintaining a close to constant magnitude, whereas it virtually vanishes in other cases.

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The drive toward ever smaller ferroelectric devices<sup>1</sup> has resulted in nanosystems such as nanowires,<sup>2,3</sup> nanotubes,<sup>4–6</sup> and nanodots.<sup>7,8</sup> It was initially assumed that as the size of such nanoshapes continued to decrease, the ferroelectric polarization would vanish: ferroelectricity is a collective phenomenon after all. However, seminal works by Fu, Bellaiche, and Naumov<sup>9,10</sup> suggested that, before vanishing, the polarization may first undergo a size-induced transition by which the dipoles form a ferroelectric vortex, a polar configuration that does not exist in bulk and persists down to very small diameters. This insight has triggered much work, both theoretical<sup>11–17</sup> and experimental<sup>18–20</sup> toward establishing true critical diameters for ferroelectricity, characterizing the vortices, and establishing their existence.

In the present work, we have used *ab initio* methods to calculate the polar configuration in ultrathin nanowires of the archetypal ferroelectric BaTiO<sub>3</sub> (BTO). Our results show that the topological landscape of the polarization field  $\vec{P}(\vec{r})$  in nanowires is more complex than hitherto assumed, with polar configurations other than vortices appearing. The field textures obtained include saddle points<sup>17</sup> and quadrupoles as well as more complex configurations, all of them well described within the classic framework of topological point defects.<sup>21</sup> Such patterns are induced by the surfaces and can be understood in terms of simple surface and edge effects. The several surface terminations presented below illustrate the richness of textures to be expected (and possibly manipulated) when controlling the surface chemistry (not limited to the examples below).

The two-dimensional (2D) topology of the polarization field in thin nanostructures can be mapped onto the topology of  $(P_x, P_y)$  for wires if the field remains constant along  $z$ , the axial direction of the wire. This Brief Report focuses on topological defects in such 2D field<sup>21</sup> (these so-called “defects” do *not* refer to structural defects of the wires). The possible textures of the field varying along  $z$  could also be rich and interesting but are beyond the scope of this work. The winding number (or topological charge) is defined as  $n = \phi/2\pi$ , being  $\phi$  the total angle the 2D field vector rotates

when going around a closed circuit. For a continuous field,  $n$  must be an integer, which if different from zero implies the existence of at least one topological defect within the circuit. Any smooth deformation of a vector field will conserve  $n$  while changing the winding number implies a dramatic, extended, and highly energetic rearrangement.<sup>22</sup> Such  $\Delta n \neq 0$  rearrangements have been used to define “phase transformations”<sup>23</sup> for nano-objects displaying vortices ( $n = +1$ ). Here we find realizations of  $n=0, 1, -1$ , and  $-3$ . We see textures that were described before (e.g., radial ones<sup>24</sup> and several of the ones recently proposed in Ref. 17) together with other textures. The different textures are induced (and thus can be manipulated) by the different surface terminations of the wires.

Our calculations were performed within density-functional theory (DFT) and the generalized gradient approximation (GGA).<sup>25</sup> We used the SIESTA method,<sup>26,27</sup> based on finite-range numerical atomic orbitals, using a double- $\zeta$  polarized basis set.<sup>11,28</sup> Norm-conserving pseudopotentials were used, including into the valence, the semicore shells  $3s$  and  $3p$  for Ti and  $5s$  and  $5p$  for Ba. The performance of the method was tested for bulk BaTiO<sub>3</sub>. The obtained lattice parameter for the rhombohedral phase is 0.12% smaller than the experimental value of 4.0036 Å at 15 K,<sup>29</sup> and 0.055% smaller than the published results with the same GGA and plane waves as basis set.<sup>25</sup> The rhombohedral angle was found to be 89.84°, exactly as obtained in the same experiments, and the off-centering of the Ti atom came out as 0.184 Å, as compared with the experimental 0.185 Å. Periodic boundary conditions were used with a simulation cell describing a square array of infinite nanowires, such that periodic replicas are separated by 24 Å. The width of the wires is shown in Fig. 1. The unit cell along the wire axis comprises a single bilayer in all cases, and therefore all polarization textures are homogeneous along  $z$  by construction. Integrals in reciprocal space used a  $\vec{k}$  mesh of 10 Å cutoff<sup>30</sup> while the integrals in real space used a  $\vec{r}$  mesh of 350 Ry cutoff,<sup>27</sup> converging energies within 0.3 meV/atom and off-center displacements within 0.5 pm. The atomic positions

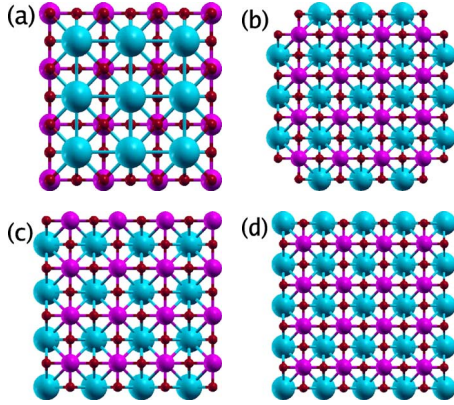


FIG. 1. (Color online) Sections of the different  $\text{BaTiO}_3$  nanowires considered. The largest balls (cyan) are for Ba ions, the intermediate ones (magenta) represent Ti ions, and the smallest ones (red) are for O. (a) is  $\text{TiO}_2$  terminated, (b) is BaO terminated, except the edges, where lines of Ba atoms have been removed, and (c) is stoichiometric, with two BaO surfaces and two  $\text{TiO}_2$  ones. (d) is BaO terminated.

were relaxed until all atomic force components were smaller than  $10 \text{ meV}/\text{\AA}$ , and the cell size along  $z$  was varied until all stress components were below  $0.1 \text{ kbar}$ . All the structures described below correspond to the lowest energy found in each case. Unpolarized or uniformly polarized wires were found to be unstable. Symmetry-breaking instabilities doubling or tripling the cell size along the wire were not found in further relaxations.

From the relaxed structures, the Ti displacement from the center of its coordination octahedron was taken to define  $\vec{P}(\vec{r}_{\text{Ti}})$ , as a measure of the local dipole. For Ti atoms on surfaces or edges, the off-center displacement was determined by the remaining coordinating O atoms. The results and discussions presented below refer to such off-center displacements. It should be emphasized, however, that the focus of the Brief Report is on the topological aspects of the field texture and their consequences. Although there are known discrepancies between off-centerings and local dipoles [see the BaO-terminated (001) BTO surface<sup>31</sup>], the existence and implications of different topological defects should not be affected by them.

Four different kinds of nanowires have been considered, corresponding to different surface terminations, as shown in Fig. 1, all showing (100) and (010) surfaces, or slight alterations thereof. Two of them display the same termination on all sides, namely, (a) all  $\text{TiO}_2$  terminated or (d) all BaO terminated. (c) Wire type is stoichiometric, with both terminations, and corresponding to the wires studied in Ref. 11. Finally (b) is like (d) except for the fact that the Ba on the edges has been removed. Each wire type has been considered in several sizes, mainly  $4 \times 4$  and  $5 \times 5$ , counting the Ti atoms.

Figure 2 shows the textures of the wire types of Fig. 1, alongside qualitative sketches of the corresponding topological defects for a 2D vector field. The discrete set of off-centering vectors is assimilated to a lattice discretization of a 2D field. Different wire widths correspond to different discretizations of the same pattern. A first striking result is that

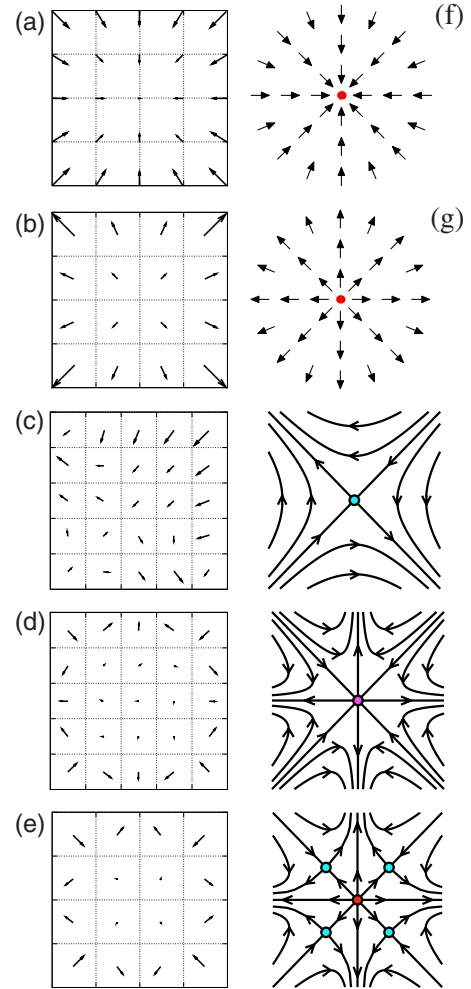


FIG. 2. (Color online) Left (a)–(d): Ti off-center displacements for the four types of nanowires in Fig. 1. (e) is analogous to (d) but for a thinner wire. Right: sketches of corresponding 2D field lines around topological point defects of winding numbers  $n=1$ ,  $1$ ,  $-1$ , and  $-3$ , respectively. (j) shows  $n=-3$  decomposing into one  $n=+1$  and four  $n=-1$  defects. The respective largest arrows correspond to (a)  $21 \text{ pm}$ , (b)  $35 \text{ pm}$ , (c)  $23 \text{ pm}$ , (d)  $6.8 \text{ pm}$ , and (e)  $6.6 \text{ pm}$ .

even for the small sizes considered (and the coarse discretization they imply), the field textures appear very clearly. All textures preserve inversion symmetry at the center of the wire if it was not previously broken by the surface termination. The first two cases in Fig. 2, displaying inward and outward radial patterns, correspond to the same kind of topological defect, of winding number  $1$ . They are thus homotopical with each other but also with the vortex structures seen in Refs. 10, 13, and 17. The continuous transformation taking a radial texture onto a vortex one is beautifully illustrated in Mermin's review.<sup>21</sup> They of course differ in other physical aspects, such as the nonzero toroidal moment of the vortex patterns.

Figures 2(c) and 2(d) correspond to two different winding numbers,  $-1$  and  $-3$ , the latter not yet observed or proposed in this field. In Fig. 2(c), the defect is displaced from the center (it is the only noncentrosymmetric wire). Figure 2(d) shows the  $n=-3$  case of the BaO-terminated wire. The high winding number imposes a more rapidly varying field around

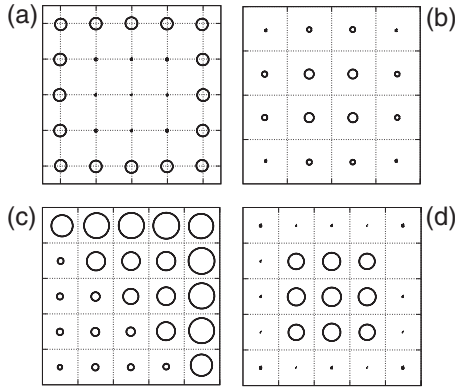


FIG. 3.  $z$  component of the Ti off-centering for the wires in Fig. 1. The largest circle represents a value of 15 pm.

the defect, which implies higher energy. The system responds by a more pronounced depression of the magnitude of the 2D field around the defect. The winding of the field around the outer circuit in the wire section clearly corresponds to  $n=-3$ .

Figure 2(e) is for the same BaO termination as Fig. 2(d) but smaller thickness. Although a different discretization, the winding around the outer circuit clearly shows the same  $n=-3$ . In this case, the inner displacements, although small, all point mainly outward, inconsistently with the  $n=-3$  texture. This system has found more stability in decomposing the global  $n=-3$  global defect into a set of defects whose winding numbers add up to  $-3$ . In general,<sup>21</sup> when following the winding of the field around a circuit, the winding number obtained is the sum of winding numbers of all the point defects enclosed in the circuit. In this case, the texture can be described by a central defect with  $n=+1$ , the field radiating outward as in Fig. 2(g), plus four other defects of  $n=-1$ , as illustrated in the last sketch.

The described textures are clearly induced by surface and edge effects. Indeed, the phenomenology described can be understood as originated by three simple tendencies: (i) in Ti-terminated surfaces and edges, the Ti atoms tend to off-center inward, (ii) Ba surface termination induces outward Ti off-centering patterns while (iii) Ba edge termination induces an inward tendency. The competition of (ii) and (iii) in the Ba-terminated wires gives rise to the rich  $n=-3$  pattern. By removing the Ba edges [Fig. 2(b)], the competition disappears and the fully outward pattern is established. Similarly, when removing the Ba edge in the stoichiometric case, the polarization field becomes topologically homogeneous ( $n=0$ ), with the field lines crossing the wire diagonally pointing left and down (not shown). Special chemical tendencies at edges and surfaces have been previously reported.<sup>16–18</sup> Shimada *et al.*<sup>16</sup> talk specifically about strong “edge bonds” for PbTiO<sub>3</sub> nanowires. We do not further analyze the electronic effects originating those tendencies, however, since the particular chemistries illustrated here are only examples of a much larger set of possibilities to be exploited in experiments.

The surfaces not only determine the  $(P_x, P_y)$  topology but also the  $P_z$  behavior (Fig. 3). Axial switchable polarization has been observed experimentally,<sup>19</sup> and has been analyzed

within Landau-Ginzburg theory<sup>12,14</sup> and DFT.<sup>11,16,17</sup> We find that for TiO<sub>2</sub> termination, the  $4 \times 4$  wires display  $P_z=0$  while it is finite for  $5 \times 5$  (in the figure) or larger. When nonzero, the axial polarization stems mainly from the surface cells, the central cells displaying much smaller displacements. This is surprising: an essentially constant-magnitude field is commonly assumed for these and other ferroelectric systems (some models have this assumption built in, as a constant dipole moment of arbitrary orientation). Here, however, the field responds by vanishing smoothly into the defect. The BaO-terminated wires respond in the more expected way: discontinuity at the defect is avoided without substantial diminishing of the polarization field, by having maximal axial polarization at the wire center. This is the case for both with and without Ba edges, although the latter shows a much smaller axial component at the center. There is also a  $3 \times 3$  critical thickness for  $P_z$  (largest system with  $P_z=0$ ) in the Ba-terminated case. In the stoichiometric wires, the situation is different. The figure shows a  $5 \times 5$  case (the critical thickness for this type is  $2 \times 2$ , in agreement with Ref. 11), which again shows large  $P_z$  for the surface and edge Ti displacements, for which the in-plane components were also large.

In addition to their intrinsic fundamental interest, the polarization-field textures and the possibility of manipulating them, offer interesting exploitation possibilities. Net polarization has been measured and switched perpendicularly to the wire axis at room temperature with a scanning probe microscope.<sup>2,3,18</sup> Such a setup should thus respond as a three-state system, with  $+1$ ,  $0$ , and  $-1$  states, the  $+1$  and  $-1$  corresponding to the conventional ferroelectric response, and the zero to the stable topologically defective state (with  $|P|$  much smaller than for the other states, strictly zero if the unpolarized wire is centrosymmetric). The field rearrangement needed for a nonhomotopical change in texture would mean an energy barrier when changing the net polarization, giving a scenario analogous to a first-order phase transition above the transition temperature: the global minimum for  $P \sim 0$  and two local minima for  $+$  and  $-$ . Note that some of the  $n \neq 0$  textures exhibit net quadrupoles. These configurations can be switched (destabilized) by application of an electric field gradient, which could, in principle, be used for a quadrupole memory device.

Phase transformations were already proposed for vortex structures in nanodots.<sup>10</sup> In wires, as extended systems, the expression would be more appropriate except for the fact that wires with sufficiently short-ranged interactions do not sustain spontaneous symmetry breaking at any finite temperature.<sup>32</sup> Even assuming that the long-range dipole-dipole interactions and the also long-ranged strain-mediated interactions do not invalidate the previous argument, the discussions in this Brief Report can be understood in terms of the observed wires being of lengths smaller than the dipole-dipole correlation length: any perturbation pins the order parameter (the polarization across wires is experimentally observed after all). As a final remark, the surface and edge control not only affects the polarization *across* the wires but can also determine the conductance *along* the wire since the deviations from  $(\text{BaO})_x(\text{TiO}_2)_y$  compositions give rise to doped wires, opening still further possibilities for these systems, to be explored elsewhere. Evidently, different surface

chemistries than the ones contemplated here can be achieved depending on how the wires are produced. The points remain, however, that interesting topologies are to be expected in thin ferroelectric wires, and that they are induced by the surfaces and edges. In addition to these, arrays of wires also offer the possibility of manipulating polarization by choosing the array lattice and its lattice parameters.

In summary, using first-principles calculations we obtain ferroelectric patterns in BTO nanowires for different surface terminations, with textures that correspond to the topological

winding numbers  $n=0, +1, -1$ , and  $-3$  of topological point defects in 2D vector fields. A tendency of the  $n=-3$  defect to decompose into one  $+1$  and four  $-1$  defects is observed, as well as the different mechanisms used by the field to avoid discontinuities.

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